

Non-topological edge-localized Yu-Shiba-Rusinov states in CrBr₃/NbSe₂ heterostructures

Jan P. Cuperus, Daniel Vanmaekelbergh and Ingmar Swart*

Debye Institute for Nanomaterials Science, Utrecht University, The Netherlands

* i.swart@uu.nl

Abstract

Topological superconductivity is predicted to emerge in certain magnet-superconductor hybrid systems. Here, we revisit the heterostructure of insulating monolayer CrBr₃ and NbSe₂, for which different conclusions on the presence of topological superconductivity have been reported. Using low-temperature scanning tunneling microscopy and (shot noise) spectroscopy, we find that the superconducting gap well inside the CrBr3 islands is not affected by magnetism. At the island edges, we observe Yu-Shiba-Rusinov (YSR) states at a variety of in-gap positions, including zero energy. The absence of topological superconductivity is verified by extensive dI/dV measurements at the CrBr₃ island edges. Our results ask for a more detailed understanding of the interaction between magnetic insulators and superconductors.

© O Copyright J. P. Cuperus et al. This work is licensed under the Creative Commons Attribution 4.0 International License. Published by the SciPost Foundation.

Received 2025-01-27 Accepted 2025-04-08 Published 2025-04-28



doi:10.21468/SciPostPhys.18.4.141

Contents

1	Introduction	2					
2	2 Methods						
3	Results and discussion	4					
	3.1 Morphology & structure	4					
	3.2 Electronic characterization	4					
	3.3 SC gap characterization	6					
	3.4 Further characterization of YSR edge states	8					
	3.5 Further characterization of SC gap on CrBr ₃ by shot noise spectroscop	y 8					
4	Conclusions						
Α	Extended data						
	A.1 Mirrored CrBr ₃ orientation on adjacent NbSe ₂ planes	11					
	A.2 McMillan fitting of SC gap	11					
Re	References						



1 Introduction

At present, the road to scalable quantum computing is cumbersome due to the qubit decoherence problem [1,2]. Despite recent advancements in quantum error correction, the decoherence problem requires large physical and technological overhead [3,4]. The development of topological qubits, which have significantly lower decoherence rates, would therefore be a leap forward towards scalable quantum computing. Central to the working principle of topological qubits are Majorana zero-modes (MZMs), exotic fermionic particles that obey non-Abelian statistics [5, 6]. As a potential platform for the realization of MZMs, topological superconductors are actively sought after in condensed matter systems. Examples of material systems that have shown signs of MZMs include proximitized semiconductor nanowires [7–10], proximitized topological insulators [11–14], superconducting topological surface states [15, 16], and 1D/2D magnetic lattices on superconducting surfaces [17-23]. In the examples above, topological superconductivity (TSC) is established by the induced, effective p-wave pairing of superconductivity; the required spin degeneracy lifting is provided by a topological phase transition [5], as has been shown for lattices of Yu-Shiba-Rusinov (YSR) states [23]. YSR states are in-gap bound states induced by the exchange interaction between magnetic atoms (historically: impurities) and Cooper pairs [24-27]. In the classical spin approximation [28], the energy of YSR states (E_{YSR}) with respect to the Fermi level (E_F) depends on the exchange coupling J and the impurity spin S_{imp} :

$$E_{\rm YSR} = \Delta \frac{1 - a^2}{1 + a^2}$$
, with $a = JS_{\rm imp} \pi \rho_s$. (1)

Here, Δ is the superconducting gap size and a parameterizes the impurity-substrate interaction via J, $S_{\rm imp}$, and ρ_s , which is the density of states of the substrate at $E_{\rm F}$ in the normal state. From Eq. (1), it follows that YSR states may be localized at $E_{\rm F}$, in which case they would be indistinguishable from a MZM in density of states measurements. This implies that a zero-bias peak (ZBP) in a density of states measurement is no definitive proof of MZMs (or TSC). Other arguments are thus required to label a ZBP as a MZM. For example, plateaus at quantized conductance values in transport experiments would support a MZM claim [29, 30].

Recently, the existence of a ZBP at the edges of CrBr₃ islands, grown on NbSe₂, has been interpreted as a 1D MZM [31]. It is reasoned that the magnetic insulator CrBr₃ interacts with the *s*-wave superconductivity of the NbSe₂ substrate, leading to YSR bands that are in a topological phase, thanks to a moiré potential [32]. The ZBP observation is supported by an extensive theoretical model, which can also explain the observed interruptions of the 1D MZM. Given the impact of this finding, we set out to confirm these observations and improve the understanding of this exciting material platform. Here, we report independent STM measurements of CrBr₃/NbSe₂ heterostructures, grown by MBE. In contrast to refs. [31,32], we find no YSR bands in the interior of the CrBr₃ islands, and no 1D ZBP at the edges. Instead, we find edge-localized YSR states, whose energies are spread across the superconducting gap (including very close to zero energy). The YSR states disperse along small edge segments, and the YSR state energy can be tuned by interaction with the STM tip. Our findings are in excellent agreement with the recent report of Li et al. [33], which was published shortly after our experiments had been performed.



2 Methods

Sample preparation

The growth of $CrBr_3$ thin films was performed in an ultra-high vacuum chamber with a base pressure of ca. 5×10^{-10} mbar. A $NbSe_2$ single crystal (HQGraphene), glued to a molybdenum sample holder with conductive epoxy (EpoTek H20E), was used as the substrate. The $NbSe_2$ surface was prepared by cleaving, using scotch tape, in the fast entry lock (pressure lower than 4×10^{-8} mbar). Prior to cleaving, the $NbSe_2$ sample was degassed up to $300\,^{\circ}$ C. $CrBr_3$ was evaporated from an e-beam evaporator (EFM3, Focus GmbH) containing a $CrBr_3$ single crystal (HQGraphene) in a quartz cup. A sub-monolayer coverage of crystalline $CrBr_3$ islands was obtained by evaporating for 6 min onto a freshly cleaved $NbSe_2$ crystal, which was heated to $230\,^{\circ}$ C. After growth, the sample was kept at the growth temperature for 15 min. After cooldown, the sample was transferred to the STM head, which is part of the same ultra-high vacuum system.

STM/STS measurements

All scanning tunneling microscopy (STM) and scanning tunneling spectroscopy (STS) measurements were performed using a USM1300 (Unisoku Co. Ltd.), operated at $T=360\,\mathrm{mK}$. The electronic temperature of our system is ca. $500\,\mathrm{mK}$, as estimated from fitting of the SC gap of NbSe₂ (see Appendix A.2 for fits). A mechanically polished PtIr wire, conditioned on Au(111), was used as the STM tip. In STS experiments, dI/dV signals were recorded by lock-in detection, using a modulation frequency of either 771 Hz or 971 Hz. Modulation amplitudes $V_{\rm ac}$ are given in the description of each experiment. STM and STS data was organized using SPMImageTycoon [34]; STM images were analyzed using Gwyddion [35].

Shot noise measurements

We have measured the shot noise generated by the tunneling current at MHz frequency using a recently developed amplification circuit [36]. In essence, the circuit consists of a bias tee, a superconducting LC resonator ($f_0=2.8\,\mathrm{MHz}$, $Q\approx1800$), and a high-electron-mobility transistor (HEMT). The bias tee is used to separate low frequency signals (STM feedback, dI/dV signal) from high frequency signals, whereas the LC resonator converts current noise from the junction into voltage noise at the gate of the HEMT. Lastly, the HEMT is used to match the high impedance circuit to the 50 Ω impedance of a transmission line. All these components are located in the vicinity of the 1 K pot, such that their temperature is expected to be < 2 K during the measurements at 360 mK ($T_{1\mathrm{K}}\sim1.6\,\mathrm{K}$). At room temperature, the noise signal is amplified by a +40 dB current amplifier (Femto HSA-X-1-40), before it is measured by a digital spectrum analyzer (MFLI, Zurich Instruments AG).

In a shot noise spectroscopy experiment, the magnitude of shot noise is measured at a set of bias voltages. In this report, shot noise spectroscopy was performed with the STM feedback configured to maintain a constant junction resistance $R_J = V_b/I$. We note that this implies a non-constant transparency of the tunnel junction, in the case of a non-constant density of states (such as a SC gap). To find the shot noise magnitude S_I , the power spectral density $S_V(\omega)$ is measured in a 100 kHz bandwidth around the resonator's center frequency, using lock-in detection (zoom FFT). For each bias point, the current noise is extracted from a fit of $S_V(\omega)$ using a simplified model of the circuit:

$$S_{V}(\omega) = S_{\text{tot}} \times |Z_{\text{tot}}(\omega)|^{2} + S_{V}^{0}, \tag{2}$$



where $Z_{\rm tot}(\omega)$ is the complex impedance of the resonator circuit, in parallel with the junction resistance $R_{\rm J}$, and $S_{\rm V}^0$ is the background (input) voltage noise level. The resonator circuit is approximated by two parallel, identical RLC resonators ($R \sim 1\,\Omega, L = 120\,\mu{\rm H}, C \sim 26\,{\rm pF}$), separated by a coupling capacitor ($C_{\rm c} = 100\,{\rm pF}$). The fit parameters are $S_{\rm tot}$, $S_{\rm V}^0$, R and C. $S_{\rm tot} = G^2\left(S_{\rm I} + S_{\rm I}^0\right)$ is the total current noise, with G being the gain of the amplification chain and $S_{\rm I}^0$ being the background current noise level. The effective charge $Q_{\rm eff}$ is extracted from the obtained $S_{\rm tot}(V_{\rm b})$ values using

$$S_{\text{tot}} = G^2 \left[2Q_{\text{eff}} |I| \times \coth\left(\frac{Q_{\text{eff}} V_{\text{b}}}{2k_{\text{B}} T}\right) + S_{\text{I}}^0 \right], \tag{3}$$

where the Schottky formula for shot noise is recognized as $2Q_{\rm eff}|I|$, and the coth-term accounts for thermal equilibrium noise of the tunnel junction [37]. Equation (3) is fitted to $S_{\rm tot}(V_{\rm b})$ for bias points where the effective charge $Q_{\rm eff}$ is known to be 1e, i.e., outside the SC gap. We find a gain G of 0.176 (excluding room temperature amplification), whereas $S_{\rm I}^0$ is ca. $50\,{\rm fA}^2/{\rm Hz}$. In our analysis, the thermal noise $S_{\rm I}^{\rm th}=4k_{\rm B}T/Z_{\rm tot}$ is included in $S_{\rm I}^0$ and not taken into account in the resonance circuit fit. By measuring each $S_{\rm V}(\omega)$ for ca. 10 min (4000 FFT repetitions), we can determine $S_{\rm I}$ to within 0.05-0.06 fA $^2/{\rm Hz}$ [95% confidence interval, based on uncertainty in $S_{\rm V}(\omega)$], nearly independent of current/bias. This uncertainty is taken into account in the calculation of $Q_{\rm eff}$, for which the confidence interval becomes larger for smaller currents, because of a lower signal-to-noise ratio.

3 Results and discussion

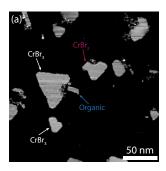
3.1 Morphology & structure

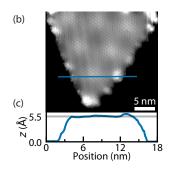
Figure 1a shows the typical morphology of the as-grown $CrBr_3/NbSe_2$ heterostructure. $CrBr_3$ has formed monolayer islands of triangular shape, which vary in size from 10 nm to 60 nm. The islands have an apparent height of $\sim 5.5\,\text{Å}$ at $V_b = +1.5\,\text{V}$ (5.0 Å at $V_b = 0.9\,\text{V}$), indicative of their monolayer thickness. In addition to the $CrBr_3$ islands, the evaporation process has introduced some organic contaminants, visible as elongated structures (annotated in blue). Small patches of $CrBr_2$ are also observed (annotated in red), always attached to $CrBr_3$ islands and indicative of slight $CrBr_3$ degradation [38].

On the $CrBr_3$ islands, a moiré pattern is visible, resulting from the lattice mismatch between $CrBr_3$ and $NbSe_2$ (see Fig. 1b). The moiré pattern has a periodicity of $6.1\,\mathrm{nm}\pm0.1\,\mathrm{nm}$, which is similar to what has been reported previously [31,33]. Furthermore, Fig. 1b shows that the $CrBr_3$ island is crystalline in the interior, but that the edges are not atomically straight – also in line with the previous reports. In an STM topograph with atomic contrast, shown in Fig. 1c, the moiré lattice can be observed together with the characteristic atomic pattern of $CrBr_3$. The moiré pattern is not exactly aligned with the rows of Br atoms, showing that the twist angle is not exactly 30° (as suggested in previous reports), but closer to 32° . Additionally, we observed that $CrBr_3$ islands on adjacent $NbSe_2$ planes, which have mirrored sublattice symmetries, have a mirrored orientation (see Fig. A1). This indicates that the twist angle is (in part) determined by the atomic interaction between the substrate and the epilayer.

3.2 Electronic characterization

We have investigated how the magnetic insulator $CrBr_3$ affects the electronic structure of $NbSe_2$ via STS experiments inside the band gap of $CrBr_3$. By measuring inside the band gap, STS experiments can probe the $NbSe_2$ density of states (DOS) beneath the $CrBr_3$ islands. To study charge transfer effects, we recorded STS data in the energy range from $V_b = -0.5 \, \text{V}$ to





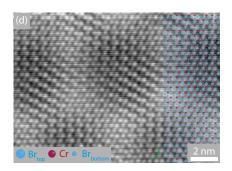
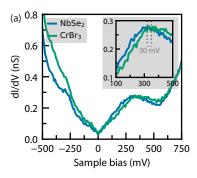
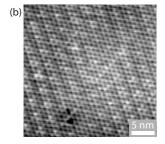


Figure 1: Structure of as-grown $CrBr_3/NbSe_2$ heterostructures at different length scales. (a) Morphology of the sample, showing that the $CrBr_3$ islands of different sizes coexist with small patches of $CrBr_2$ and some organic residue. Set point: $+0.9\,V$, $50\,pA$. (b) Image of a single $CrBr_3$ island, on which both the atomic and moiré unit cells can be recognized. Set point: $+1.5\,V$, $50\,pA$. (c) Line profile measured along the blue line shown in (b). The apparent height of the $CrBr_3$ island is $5.5\,\text{Å}$. (d) Image of the $CrBr_3$ lattice with atomic resolution: individual Br atoms are visible, as well as the moiré pattern. An atomic model of the $CrBr_3$ lattice is overlaid. Set point: $+0.93\,V$, $50\,pA$.





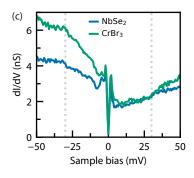


Figure 2: Characterization of the electronic structure of $CrBr_3/NbSe_2$. (a) dI/dV spectrum probing the charge transfer from $NbSe_2$ to $CrBr_3$. The Nb d-band at $+300\,mV$ shifts by ca. $+30\,mV$, indicative of slight electron doping of $CrBr_3$. Set point: $1\,V$, $200\,pA$, $V_{ac}=9\,mV$. (b) STM image showing the CDW of $NbSe_2$. Set point: $+200\,mV$, $100\,pA$. (c) dI/dV spectrum probing the CDW of $NbSe_2$ beneath a $CrBr_3$ island. Set point: $+100\,mV$, $300\,pA$, $V_{ac}=0.65\,mV$.

 $V_{\rm b} = +0.75\,\rm V$. By comparing data acquired on the CrBr₃ islands to data recorded on NbSe₂, we have found that the CrBr₃ induces a shift of ca. $+30\,\rm mV$ of the Nb d-band at $V_{\rm b} \sim +300\,\rm mV$. This shift has been interpreted as a sign of electron doping from NbSe₂ to CrBr₃ and is, given the uncertainty, similar in magnitude to what has been reported by refs. [31] and [33].¹

In the smaller bias range from $V_b = -100\,\mathrm{mV}$ to $V_b = +100\,\mathrm{mV}$, we have used STS experiments to probe the charge density wave (CDW) beneath the CrBr₃ islands. Away from the islands, the CDW is readily visible in STM topographs such as Fig. 2b. In STS, the CDW is manifested as kinks at ca. $\pm 35\,\mathrm{mV}$ [39]. As shown in Fig. 2c, we indeed observe a change of slope around $\pm 30\,\mathrm{mV}$, both on NbSe₂ (blue curve) and on CrBr₃ (green curve).

 $^{^{1}}$ Ref. [31] reports a shift of +80 mV based on a contour plot, but from the line plot a value of +30 mV seems more appropriate.



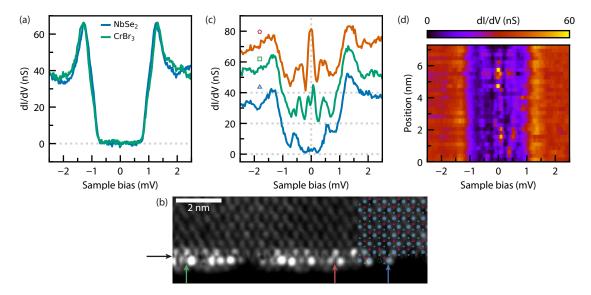


Figure 3: (a) SC gap of NbSe $_2$ (green) and CrBr $_3$ (blue). A hard SC gap is observed on both locations. (b) Constant height image of the edge segment probed by the STS experiments shown in (c), (d). Set point: $+5\,\mathrm{mV}$, $50\,\mathrm{pA}$. (c) Selected spectra from the line spectrum shown in (d), displaying the variety of in-gap profile found on a single edge segment. Locations of the spectra are indicated in (b). Spectra are offset vertically by 20 nS for clarity. (d) Contour plot of dI/dV spectra acquired along a line on the edge shown in (b). The location of the line spectrum is indicated by the black horizontal arrow in (b). Set points for (a), (c) and (d): $+5\,\mathrm{mV}$, $150\,\mathrm{pA}$, $V_{ac} = 33\,\mu\mathrm{V}$.

3.3 SC gap characterization

To investigate the effect of $CrBr_3$ on the superconductivity of $NbSe_2$, we performed STS experiments in a small bias window around E_F . First, we compared the SC gap measured on the $CrBr_3$ islands to measurements on bare $NbSe_2$. We find that the SC gaps measured on both locations are nearly identical, as shown in Fig. 3a. In contrast to ref. [31], but in line with ref. [33], no YSR bands are found in the interior of the $CrBr_3$ islands. As a more detailed analysis, we have fitted the data of several $NbSe_2$ and $CrBr_3$ SC gaps using the McMillan model [40,41], but we do not observe a trend in the fit parameters indicative of YSR bands (see Appendix A.2). An investigation of the superconductivity in the interior of the $CrBr_3$ islands by shot noise spectroscopy is presented below.

Next, we focused on the edges of the $CrBr_3$ islands. By recording constant height maps, we have mapped the atomic structure of an edge (see Fig. 3b). In the interior of the island, the Br sublattice can be observed, from which we can extract the orientation of the $CrBr_3$ lattice (see the atomic model overlaid in Fig. 3b). From the orientation, it follows that the edge corresponds to the armchair edge of the honeycomb sublattice formed by the Cr atoms. Even in close vicinity of the edge, the $CrBr_3$ crystallinity is pristine; only in the last unit cell (\sim 6Å), the atomic structure is more disordered, and in some parts, missing atoms can be identified. However, in other edge segments, the $CrBr_3$ lattice appears intact, except for the unavoidable termination of the periodicity. In such parts, the outermost $CrBr_3$ atoms are only faintly visible. The low intensity of these $CrBr_3$ atoms suggests that they are bent downwards (towards the substrate), although we cannot rule out that this effect stems from the electronic structure instead. Either way, the presence of these $CrBr_3$ island.



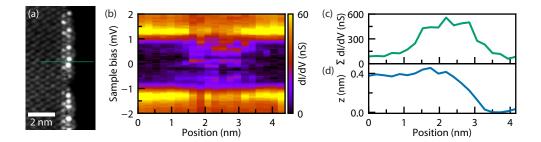


Figure 4: (a) Constant height map of a CrBr $_3$ island edge. The green line indicates the position of the line spectrum, which is shown in (b). Set point: +5 mV, 50 pA. (b) Line spectrum measured across a CrBr $_3$ edge. In-gap states are observed in a 2 nm wide region close to the edge. Set point: +5 mV, 150 pA, $V_{ac} = 33 \,\mu\text{V}$ (c), (d) Summed in-gap dI/dV signal and tip height of the line spectrum shown in (b).

The constant-height current map (Fig. 3b) shows clear intensity variations along the edge. To explain this observation, we turn to the spectroscopy data acquired on this edge. $\mathrm{dI/dV}$ spectra acquired on positions that have different intensities in Fig. 3b exhibit very different in-gap features. The in-gap features come in pairs, which appear symmetrically around E_{F} , but are asymmetric in intensity. Based on the energy symmetry, we interpret the peak pairs to be YSR states. We note that these YSR states most likely do not result from undercoordinated Cr atoms at the edge, as the atomic structure is pristine (as discussed above). Instead, we expect the YSR states to arise from a Cr 3d DOS at E_{F} that is increased at the edge, as we have reported for $\mathrm{CrCl_3/NbSe_2}$ [42]. The increased DOS strengthens the exchange interaction between the Cr atoms and the NbSe₂ substrate, and can explain the edge-localization of the YSR states.

Depending on position, the main YSR states can be located close to the coherence peaks (bottom curve), close to E_F (middle curve), or precisely at E_F (upper curve). In the latter case, the YSR states are so close in energy that only a single peak is observed at $E_{\rm F}$. This happens despite the fact that in-gap states observed here have a smaller full-width at half maximum than those reported in ref. [31]. Not only the energy, but also the intensity of the YSR states can vary greatly, independent on the YSR state energy. To characterize the edgelocalized YSR states more systematically, we have recorded a line spectrum along the edge (see the contour plot in Fig. 3d). The line spectrum shows that the YSR state energies vary smoothly with position, indicative of coupling between the individual YSR states. The coupling also extends across the low-intensity segment at ca. 3 nm from the left. The fact that the peak positions vary spatially, and are not pinned to zero energy, rules out the presence of topological superconductivity in our experiments. Instead, the YSR states are more likely to originate from the (magnetic) Cr atoms at the edge, similar to what we have observed for CrCl₃/NbSe₂ [42]. For that material system, we find that, at the edges of the island, the LDOS at energies close to the Fermi level is increased, strengthening the exchange interaction between the Cr atoms and the NbSe₂ substrate.

The constant height map of Fig. 3b suggests that the YSR states are localized to a region of width $\sim 1\,\mathrm{nm}$ from the edge. To confirm this edge-localization, we performed dI/dV spectroscopy on a line perpendicular to the edge. Also in this line spectrum, the in-gap states appear within a small region close to the edge (see Fig. 4b). Compared to the high-intensity region in the constant height map of Fig. 4a, the YSR states in the line spectrum appear slightly more extended to the outside of the island. We attribute this to the fact that the feedback is enabled between each position in the line spectrum.



3.4 Further characterization of YSR edge states

YSR states are sensitive to the chemical environment of the magnetic species. For example, it has been shown that the energy of YSR states is affected by the CDW of NbSe $_2$ [43] and by the moiré pattern of self-assembled molecular monolayers [44]. Here, we observed the YSR states at the CrBr $_3$ edges to be highly sensitive to the surrounding environment. In the CrBr $_3$ edge (line spectrum) shown in Fig. 3, the edge is well-ordered, resulting in an in-gap profile that changes smoothly along the edge. However, at an edge that is only slightly more disordered, we observed a variety of in-gap profiles, as shown in Fig. 5a, b. Spatially dispersive YSR states can still be recognized along small edge segments, but completely different in-gap profiles appear in adjacent segments. Most notably, the in-gap profile contains YSR states close to zero energy in the left part of the edge, whereas YSR states are only found closer to the coherence peaks in the right part.

In addition to spatial variations, the YSR state energy could also be altered by interaction with the STM tip. By recording the SC gap at varying tip-sample distances (i.e., different tunneling transmissivity), the YSR state could be tracked through the quantum phase transition [28], as shown in Fig. 5c. At the largest tip-sample distance (lowest transmissivity, bottom of Fig. 5c), the most intense YSR states are found at ± 0.2 meV. Upon decreasing the tip-sample distance (increasing transmissivity), these states shift towards $E_{\rm F}$, up until a normal state conductance of $\sim 0.3 \,\mu\text{S}$, after which the states split again. By changing the tip-sample distance, we tune the atomic forces between tip, substrate and epilayer. Presumably, the approaching tip pushes down the $CrBr_3$, thereby increasing the exchange coupling J between the Cr atom(s) and the superconducting substrate [45–47]. The exchange coupling J directly affects the YSR state energy $E_{\rm YSR}$ according to Eq. (1), which is visualized in Fig. 5d. In the weak coupling regime (small J, $a^2 < 1$), the ground state of the spin-superconductor system is a free-spin state. In this regime, the in-gap states observed at positive (negative) energy in STS experiments correspond to the excitation to the screened-spin state via the electron-like (hole-like) part of the YSR state. When the exchange coupling is increased beyond a certain magnitude $J_{\rm crit}$, the system goes through a quantum phase transition, after which the screened-spin state becomes the ground state. Beyond the phase transition, the electron- and hole-like components of the YSR state have switched sides, i.e., the electron-like part is found at negative energy, and the hole-like part at positive energy. In the STS data of Fig. 5c, this side-switching is visible by the reversal of the in-gap states' relative spectral weight. At the largest tip-sample distance, the in-gap state at negative energy is most intense, while the most intense state is found at positive energy for the smallest tip-sample distances. As may be clear from Fig. 5d, YSR states are located at $E_{\rm F}$ when J is tuned to be at the quantum phase transition ($J = J_{\rm crit}$). In the current experiment, however, the steps in tip-sample distance were too coarse to observe this point of the phase diagram. We cannot exclude that, as the tip-sample distance becomes smaller, the charge transfer between NbSe2 and CrBr3, as well as the magnetic moments, may change, which could also contribute to the experimentally observed behavior. This would be especially relevant for quantum spin systems with magnetic moments above S=1/2. Nevertheless, this experiment shows the tunability of the YSR states found at the edges of CrBr₃ islands.

3.5 Further characterization of SC gap on CrBr₃ by shot noise spectroscopy

A main difference between our data and that of ref. [31] is the absence of YSR bands in the SC gap, as probed by STS experiments inside the $CrBr_3$ islands (see Fig. 3a). To verify that the YSR bands are truly absent (and not just very small), we characterized the SC gap on $CrBr_3$ by means of regular STS experiments at varying tip-sample distance (Fig. 6a) and by shot noise spectroscopy (Fig. 6b, c). For the STS experiments, the current set point (at 5 mV) was increased from 300 pA for the largest tip-sample distance to 5 nA for the smallest tip-sample

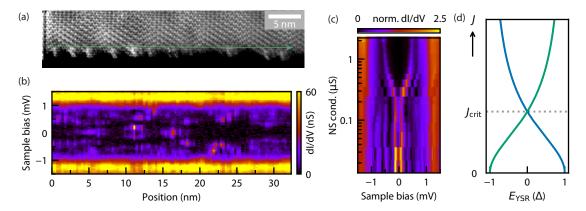


Figure 5: (a) Constant height STM image of an island edge that is longer but more disordered than the edge shown in Fig. 3b. Set point: +5 mV, 50 pA. (b) Contour plot of dI/dV spectra acquired along the green line shown in (a). In-gap states disperse along small edge segments only. Set point: +5 mV, 150 pA, $V_{\rm ac}=40$ µV. (c) Contour plot of dI/dV spectra of a YSR state, acquired at different tip-sample distances. By approaching the sample, the YSR state energy is tuned through the quantum phase transition. The normal-state (NS) conductance is defined as the average conductance signal in the bias range $|V_b|=3-5$ mV. To calculate the normalized conductance, the differential conductance is divided by the NS conductance. Set points: +5 mV, 70 pA -9 nA, $V_{\rm ac}=30$ µV. (d) Position of the YSR state energy as a function of the exchange interaction J, according to Eq. (1). The quantum phase transition occurs at $J=J_{\rm crit}$.

distance. In the resulting STS data, shown in Fig. 6a, no sign of YSR bands is observed at any tip-sample distance. Even at the smallest tip-sample distance, the SC gap is fully developed. At negative bias, a small feature can be observed inside the SC gap. We interpreted this feature as the wavefunction tail of one of the nearby ($\sim 6\,\mathrm{nm}$) edge-localized YSR states. The extension of YSR wavefunctions over such distances is possible in NbSe₂, thanks to the 2D character of its superconductivity [48].

In addition to these STS experiments, we have performed shot noise spectroscopy to check for YSR bands on CrBr₃. In shot noise spectroscopy, the magnitude of shot noise, measured as a function of the bias voltage, is used to determine the effective charge of the tunneling (quasi)particles. For a fully-developed superconducting gap, the effective charge changes from $Q_{\rm eff} = 1$ e at bias voltages outside the gap to $Q_{\rm eff} = 2$ e inside the gap, corresponding to a change in the tunneling mechanism from quasiparticle tunneling to Andreev reflections [49-52]. In tunnel junction shot noise experiments, the effective charge $Q_{\rm eff}$ at in-gap biases is very sensitive to any 1e-tunneling pathways available, such as quasiparticle poisoning by temperature or (residual) magnetic fields. In constant conductance shot noise spectroscopy experiments, as performed here, a $Q_{\rm eff}$ = 1e contribution of only 1% to the total tunnel current already reduces the effective charge from $Q_{\rm eff} = 2e$ to $Q_{\rm eff} \approx 1.1e$ [53, 54]. Here, we use this sensitivity to 1e-tunneling pathways to search for YSR bands that may be found in CrBr₃/NbSe₂. In typical STM experiments, the excitation of a YSR state is a single-electron process, which implies that tunneling events probing this excitation have an effective charge $Q_{\text{eff}} = 1e$ [55]. Hence, we expect to find an effective charge $Q_{\rm eff}$ well below 2e on $CrBr_3/NbSe_2$ if any YSR bands are present [56]. Instead, we find an effective charge of $Q_{\rm eff}=1.67e\pm0.02e$ (see Fig. 6b, c). Following ref. [53], this indicates that the contribution of 1e tunneling events is smaller than 0.1 %. The data in Fig. 6 confirm what is suggested by Fig. 3: no YSR bands exist in the CrBr₃/NbSe₂ heterostructure. Thus, the superconductivity is not affected by magnetic effects.



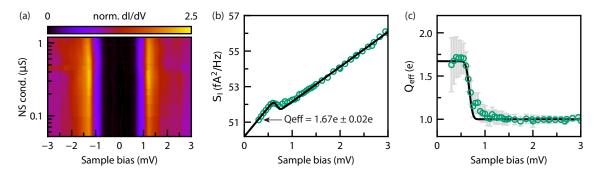


Figure 6: (a) Contour plot of dI/dV spectra measured in the interior of a CrBr3 island, acquired at different tip-sample distances. The SC gap is not affected by the tip-sample distance. The NS conductance is calculated as in Fig. 5b. Set points: +5 mV, 300 pA - 5 nA, $V_{\rm ac} = 30\,\mu\rm V$. (b), (c) Current noise $S_{\rm I}$ (b) and effective charge $Q_{\rm eff}$ (c) when tunneling into CrBr3, as determined by shot noise spectroscopy. A constant junction resistance $R_{\rm J} = 5\,\rm M\Omega$ was maintained during the experiment. Inside the SC gap, an effective charge $Q_{\rm eff} = 1.67e \pm 0.02e$ is found. Error bars in (c) indicate 95 % confidence intervals.

4 Conclusions

Two recent scanning tunneling microscopy studies have reported contrasting findings on the existence of topological superconductivity in $CrBr_3/NbSe_2$ heterostructures [31,33]. Here, we have further characterized the $CrBr_3/NbSe_2$ system by STM, STS and shot noise spectroscopy, and found no sign of topological superconductivity (in agreement with ref. [33]). The most notable difference with respect to the earlier work reporting topological superconductivity (ref. [31]) is the observation of edge-localized YSR states, instead of a peak pinned at zero energy. Furthermore, in the interior of the $CrBr_3$ islands, we observe a clean SC gap, essentially without quasiparticles (< 0.1%, as determined by shot noise spectroscopy). The spatial profile of the YSR states is reminiscent of the one we have recently observed in the related heterostructure $CrCl_3/NbSe_2$ [42]. In analogy to the case of $CrCl_3/NbSe_2$, the edge-localized YSR states presumably reflect an increase of the $Cr-NbSe_2$ exchange interaction, which occurs even at perfect, unreconstructed $CrBr_3$ edges.

At present, it is unclear what causes the absence (here, ref. [33]) or presence (ref. [31]) of in-gap states in the interior of CrBr₃ islands on NbSe₂. The difference may be caused by a different substrate-epilayer interaction (e.g., induced by strain) or, possibly, the presence of defects/impurities. Furthermore, we found a twist angle of 32° here, whereas an angle of 30° was reported previously. A different twist angle may affect the coupling between the ferromagnet and the superconductor. A systematic study into if/how the structure and properties of CrBr₃/NbSe₂ depend on the growth conditions may shed light on the origin of the different experimental observations. Additionally, more insight into topological superconductivity in CrBr₃/NbSe₂ may be obtained by the investigation of other magnetic 2D materials proximitized to s-wave superconductors.

Acknowledgments

The authors thank P. Liljeroth and S. Kezilebieke for insightful discussions.



Funding information I.S. thankfully acknowledges funding by the European Research Council (Horizon 2020 "FRACTAL", 865570). D. V. and I. S. acknowledge the research program "Materials for the Quantum Age" (QuMat) for financial support. This program (Registration Number 024.005.006) is part of the Gravitation program financed by the Dutch Ministry of Education, Culture and Science (OCW).

Author contributions I.S. conceived the project. J.P.C. performed the experiments and analyzed the data. D.V. and I.S. supervised the experiments. All authors discussed the results and contributed to writing of the manuscript.

Conflicting interests The authors report no conflicting interests.

Data availability The data used to produce the figures in this manuscript have been published and can be downloaded from [57].

A Extended data

A.1 Mirrored CrBr₃ orientation on adjacent NbSe₂ planes

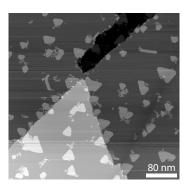


Figure A1: STM image of a location on the sample where different $NbSe_2$ terraces are observed. $CrBr_3$ islands on adjacent $NbSe_2$ terraces have opposite orientations. Set point: 0.9 V, 50 pA.

A.2 McMillan fitting of SC gap

We have fitted the SC gap, as measured on different positions on the sample and with different nanoscopic tips, using the McMillan model for two-band superconductivity. Following ref. [41], the dI/dV signal G_{tot} was fitted to:

$$G_{\text{tot}}(E) = \sum_{i=1,2} G_i \text{Re} \left[\frac{|E|}{\sqrt{E^2 - \Delta_i^2(E)}} \right],$$
 (A.1)

where G_i is the weighing factor for the two bands $i = \{1, 2\}$, and $\Delta_i(E)$ is the energy-dependent gap magnitude, which is calculated self-consistently from:

$$\Delta_{i}(E) = \frac{\Delta_{i}^{0} + a_{ij}\Delta_{j}(E)/\sqrt{\Delta_{j}^{2}(E) - E^{2}}}{1 + a_{ij}/\sqrt{\Delta_{j}^{2}(E) - E^{2}}}.$$
(A.2)



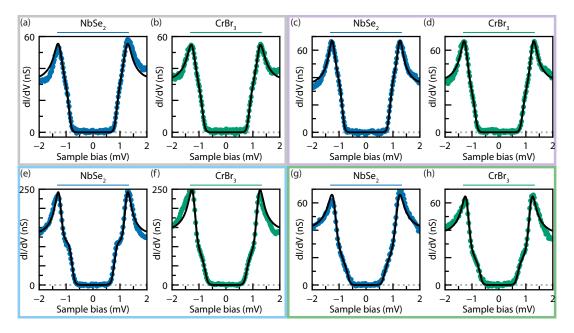


Figure A2: STS data of the SC gap on NbSe₂ and CrBr₃ positions, acquired on four different, macroscopic locations on the sample and with different nanoscopic tip. Fits to the McMillan model (Eqs. (A.1) and (A.2)) are shown as black lines. Pairs of measurements on NbSe₂ and CrBr₃, as indicated by the color coding, are performed consecutively, and with the same tip and the same measurement parameters. STM feedback was disabled at 5 mV, at a current set point of 150 pA [(a)-(d), (g), (h)] or 500 pA [(e), (f)]. Lock-in amplitude V_{ac} was either 33 μ V [(a)-(d)] or 30 μ V [(e)-(h)].

In Eq. (A.2), Δ_i^0 is the intrinsic gap in band i and a_{ij} quantifies the coupling between the two bands i and j ($i \neq j$). To include (thermal) broadening effects, Eq. (A.1) was convoluted by the derivative of the Fermi-Dirac equation with an effective temperature $T_{\rm eff}$. As shown in Fig. A2, we obtain good agreement with the experimental data. We find an effective temperature of ca. 500 mK for all datasets. From the parameters of all the fits, which are shown in Table A1, we do not observe a trend that suggests a filling of the SC gap on CrBr₃ positions.

Table A1: Optimized parameters obtained by fitting the McMillan model to dI/dV spectra of the SC gap on NbSe₂ and CrBr₃ positions. The first column ('Panel') refers to the panels in Fig. A2, where the data and the fits are shown. The parameters are introduced in Eqs. (A.1) and (A.2).

Panel	Position	$T_{\rm eff}$ (K)	Δ_1^0 (meV)	G_1 (nS)	<i>a</i> ₁₂ (meV)	Δ_2^0 (meV)	G_2 (nS)	<i>a</i> ₂₁ (meV)
(a)	NbSe ₂	0.49	1.32	26	0.54	0.0	4.5	3.37
(b)	CrBr ₃	0.50	1.31	26	0.53	0.0	4.2	3.55
(c)	NbSe ₂	0.50	1.26	23	0.28	0.0	9.4	3.32
(d)	CrBr ₃	0.50	1.29	30	0.39	0.0	4.2	3.36
(e)	NbSe ₂	0.56	1.26	75	0.17	0.0	32.7	2.20
(f)	CrBr ₃	0.53	1.24	104	0.27	0.1	7.7	2.03
(g)	NbSe ₂	0.52	1.23	32	0.35	0.0	0.0	1.96
(h)	CrBr ₃	0.53	1.22	28	0.27	0.0	0.3	1.97

12



References

- [1] P. W. Shor, *Scheme for reducing decoherence in quantum computer memory*, Phys. Rev. A **52**, R2493 (1995), doi:10.1103/PhysRevA.52.R2493.
- [2] E. Chae, J. Choi and J. Kim, An elementary review on basic principles and developments of qubits for quantum computing, Nano Converg. 11, 11 (2024), doi:10.1186/s40580-024-00418-5.
- [3] R. Acharya et al., Suppressing quantum errors by scaling a surface code logical qubit, Nature **614**, 676 (2023), doi:10.1038/s41586-022-05434-1.
- [4] R. Acharya et al., *Quantum error correction below the surface code threshold*, Nature **638**, 920 (2024), doi:10.1038/s41586-024-08449-y.
- [5] J. Alicea, New directions in the pursuit of Majorana fermions in solid state systems, Rep. Prog. Phys. **75**, 076501 (2012), doi:10.1088/0034-4885/75/7/076501.
- [6] C. W. J. Beenakker, *Search for Majorana fermions in superconductors*, Annu. Rev. Condens. Matter Phys. **4**, 113 (2013), doi:10.1146/annurev-conmatphys-030212-184337.
- [7] Y. Oreg, G. Refael and F. von Oppen, *Helical liquids and Majorana bound states in quantum wires*, Phys. Rev. Lett. **105**, 177002 (2010), doi:10.1103/PhysRevLett.105.177002.
- [8] R. M. Lutchyn, J. D. Sau and S. D. Sarma, *Majorana fermions and a topological phase transition in semiconductor-superconductor heterostructures*, Phys. Rev. Lett. **105**, 077001 (2010), doi:10.1103/PhysRevLett.105.077001.
- [9] V. Mourik, K. Zuo, S. M. Frolov, S. R. Plissard, E. P. A. M. Bakkers and L. P. Kouwenhoven, *Signatures of Majorana fermions in hybrid superconductor-semiconductor nanowire devices*, Science **336**, 1003 (2012), doi:10.1126/science.1222360.
- [10] E. Prada et al., From Andreev to Majorana bound states in hybrid superconductor-semiconductor nanowires, Nat. Rev. Phys. 2, 575 (2020), doi:10.1038/s42254-020-0228-y.
- [11] L. Fu and C. L. Kane, Superconducting proximity effect and Majorana fermions at the surface of a topological insulator, Phys. Rev. Lett. **100**, 096407 (2008), doi:10.1103/PhysRevLett.100.096407.
- [12] M.-X. Wang et al., *The coexistence of superconductivity and topological order in the Bi*₂*Se*₃ *thin films*, Science **336**, 52 (2012), doi:10.1126/science.1216466.
- [13] H.-H. Sun et al., Majorana zero mode detected with spin selective Andreev reflection in the vortex of a topological superconductor, Phys. Rev. Lett. 116, 257003 (2016), doi:10.1103/PhysRevLett.116.257003.
- [14] D. Flötotto et al., Superconducting pairing of topological surface states in bismuth selenide films on niobium, Sci. Adv. 4, eaar7214 (2018), doi:10.1126/sciadv.aar7214.
- [15] D. Wang et al., Evidence for Majorana bound states in an iron-based superconductor, Science **362**, 333 (2018), doi:10.1126/science.aao1797.
- [16] T. Machida, Y. Sun, S. Pyon, S. Takeda, Y. Kohsaka, T. Hanaguri, T. Sasagawa and T. Tamegai, *Zero-energy vortex bound state in the superconducting topological surface state of Fe(Se,Te)*, Nat. Mater. **18**, 811 (2019), doi:10.1038/s41563-019-0397-1.



- [17] F. Pientka, L. I. Glazman and F. von Oppen, *Topological superconducting phase in helical Shiba chains*, Phys. Rev. B **88**, 155420 (2013), doi:10.1103/PhysRevB.88.155420.
- [18] S. Nadj-Perge, I. K. Drozdov, B. A. Bernevig and A. Yazdani, *Proposal for realizing Majorana fermions in chains of magnetic atoms on a superconductor*, Phys. Rev. B **88**, 020407 (2013), doi:10.1103/PhysRevB.88.020407.
- [19] J. Li, T. Neupert, Z. Wang, A. H. MacDonald, A. Yazdani and B. A. Bernevig, Two-dimensional chiral topological superconductivity in Shiba lattices, Nat. Commun. 7, 12297 (2016), doi:10.1038/ncomms12297.
- [20] S. Nadj-Perge, I. K. Drozdov, J. Li, H. Chen, S. Jeon, J. Seo, A. H. MacDonald, B. A. Bernevig and A. Yazdani, *Observation of Majorana fermions in ferromagnetic atomic chains on a superconductor*, Science **346**, 602 (2014), doi:10.1126/science.1259327.
- [21] G. C. Ménard et al., *Two-dimensional topological superconductivity in Pb/Co/Si(111)*, Nat. Commun. **8**, 2040 (2017), doi:10.1038/s41467-017-02192-x.
- [22] A. Palacio-Morales, E. Mascot, S. Cocklin, H. Kim, S. Rachel, D. K. Morr and R. Wiesendanger, *Atomic-scale interface engineering of Majorana edge modes in a 2D magnet-superconductor hybrid system*, Sci. Adv. **5**, eaav6600 (2019), doi:10.1126/sciadv.aav6600.
- [23] L. Schneider, P. Beck, T. Posske, D. Crawford, E. Mascot, S. Rachel, R. Wiesendanger and J. Wiebe, *Topological Shiba bands in artificial spin chains on superconductors*, Nat. Phys. 17, 943 (2021), doi:10.1038/s41567-021-01234-y.
- [24] L. Yu, Bound state in superconductors with paramagnetic impurities, Acta Phys. Sin. 21, 75 (1965), doi:10.7498/aps.21.75.
- [25] H. Shiba, *Classical spins in superconductors*, Prog. Theor. Phys. **40**, 435 (1968), doi:10.1143/PTP.40.435.
- [26] A. Rusinov, Superconductivity near a paramagnetic impurity, J. Exp. Theor. Phys. Lett. 9, 85 (1969).
- [27] A. Rusinov, *Theory of gapless superconductivity in alloys containing paramagnetic impurities*, J. Exp. Theor. Phys. **29**, 1101 (1969).
- [28] B. W. Heinrich, J. I. Pascual and K. J. Franke, *Single magnetic adsorbates on s-wave super-conductors*, Prog. Surf. Sci. **93**, 1 (2018), doi:10.1016/j.progsurf.2018.01.001.
- [29] K. T. Law, P. A. Lee and T. K. Ng, Majorana fermion induced resonant Andreev reflection, Phys. Rev. Lett. 103, 237001 (2009), doi:10.1103/PhysRevLett.103.237001.
- [30] M. Wimmer, A. R. Akhmerov, J. P. Dahlhaus and C. W. J. Beenakker, *Quantum point contact as a probe of a topological superconductor*, New J. Phys. **13**, 053016 (2011), doi:10.1088/1367-2630/13/5/053016.
- [31] S. Kezilebieke et al., *Topological superconductivity in a van der Waals heterostructure*, Nature **588**, 424 (2020), doi:10.1038/s41586-020-2989-y.
- [32] S. Kezilebieke, V. Vaňo, M. N. Huda, M. Aapro, S. C. Ganguli, P. Liljeroth and J. L. Lado, *Moiré-enabled topological superconductivity*, Nano Lett. **22**, 328 (2022), doi:10.1021/acs.nanolett.1c03856.



- [33] Y. Li, R. Yin, M. Li, J. Gong, Z. Chen, J. Zhang, Y.-J. Yan and D.-L. Feng, *Observation of Yu-Shiba-Rusinov-like states at the edge of CrBr*₃/*NbSe*₂ heterostructure, Nat. Commun. **15**, 10121 (2024), doi:10.1038/s41467-024-54525-2.
- [34] A. Riss, *SpmImage Tycoon: Organize and analyze scanning probemicroscopy data*, J. Open Source Softw. 7, 4644 (2022), doi:10.21105/joss.04644.
- [35] D. Nečas and P. Klapetek, *Gwyddion: An open-source software for SPM data analysis*, Open Phys. **10**, 181 (2011), doi:10.2478/s11534-011-0096-2.
- [36] K. M. Bastiaans, T. Benschop, D. Chatzopoulos, D. Cho, Q. Dong, Y. Jin and M. P. Allan, *Amplifier for scanning tunneling microscopy at MHz frequencies*, Rev. Sci. Instrum. **89**, 093709 (2018), doi:10.1063/1.5043267.
- [37] H. Birk, M. J. M. de Jong and C. Schönenberger, *Shot-noise suppression* in the single-electron tunneling regime, Phys. Rev. Lett. **75**, 1610 (1995), doi:10.1103/PhysRevLett.75.1610.
- [38] S. Kezilebieke et al., Electronic and magnetic characterization of epitaxial $CrBr_3$ monolayers on a superconducting substrate, Adv. Mater. **33**, 2006850 (2021), doi:10.1002/adma.202006850.
- [39] A. Soumyanarayanan, M. M. Yee, Y. He, J. van Wezel, D. J. Rahn, K. Rossnagel, E. W. Hudson, M. R. Norman and J. E. Hoffman, *Quantum phase transition from triangular to stripe charge order in NbSe*₂, Proc. Natl. Acad. Sci. 110, 1623 (2013), doi:10.1073/pnas.1211387110.
- [40] W. L. McMillan, *Tunneling model of the superconducting proximity effect*, Phys. Rev. **175**, 537 (1968), doi:10.1103/PhysRev.175.537.
- [41] Y. Noat et al., *Quasiparticle spectra of 2H-NbSe*₂: Two-band superconductivity and the role of tunneling selectivity, Phys. Rev. B **92**, 134510 (2015), doi:10.1103/PhysRevB.92.134510.
- [42] J. P. Cuperus, A. H. Kole, A. R. Botello-Méndez, Z. Zanolli, D. Vanmaekelbergh and I. Swart, *One dimensional edge localized YSR states in CrCl*₃ *on NbSe*₂, *to be published in* npj Quantum Mater.
- [43] E. Liebhaber, S. A. González, R. Baba, G. Reecht, B. W. Heinrich, S. Rohlf, K. Rossnagel, F. von Oppen and K. J. Franke, *Yu-Shiba-Rusinov states in the charge-density modulated superconductor NbSe*₂, Nano Lett. **20**, 339 (2019), doi:10.1021/acs.nanolett.9b03988.
- [44] N. Hatter, B. W. Heinrich, D. Rolf and K. J. Franke, *Scaling of Yu-Shiba-Rusinov energies in the weak-coupling Kondo regime*, Nat. Commun. **8**, 2016 (2017), doi:10.1038/s41467-017-02277-7.
- [45] J. Brand, S. Gozdzik, N. Néel, J. L. Lado, J. Fernández-Rossier and J. Kröger, *Electron and Cooper-pair transport across a single magnetic molecule explored with a scanning tunneling microscope*, Phys. Rev. B **97**, 195429 (2018), doi:10.1103/PhysRevB.97.195429.
- [46] L. Farinacci, G. Ahmadi, G. Reecht, M. Ruby, N. Bogdanoff, O. Peters, B. W. Heinrich, F. von Oppen and K. J. Franke, *Tuning the coupling of an individual magnetic impurity to a superconductor: Quantum phase transition and transport*, Phys. Rev. Lett. **121**, 196803 (2018), doi:10.1103/PhysRevLett.121.196803.



- [47] H. Huang et al., Quantum phase transitions and the role of impurity-substrate hybridization in Yu-Shiba-Rusinov states, Commun. Phys. 3, 199 (2020), doi:10.1038/s42005-020-00469-0.
- [48] G. C. Ménard et al., *Coherent long-range magnetic bound states in a superconductor*, Nat. Phys. **11**, 1013 (2015), doi:10.1038/nphys3508.
- [49] M. J. M. de Jong and C. W. J. Beenakker, *Doubled shot noise in disordered normal-metal-superconductor junctions*, Phys. Rev. B **49**, 16070 (1994), doi:10.1103/PhysRevB.49.16070.
- [50] X. Jehl, M. Sanquer, R. Calemczuk and D. Mailly, *Detection of doubled shot noise in short normal-metal/superconductor junctions*, Nature **405**, 50 (2000), doi:10.1038/35011012.
- [51] F. Lefloch, C. Hoffmann, M. Sanquer and D. Quirion, *Doubled full shot noise in quantum coherent superconductor-semiconductor junctions*, Phys. Rev. Lett. **90**, 067002 (2003), doi:10.1103/PhysRevLett.90.067002.
- [52] K. M. Bastiaans, D. Cho, D. Chatzopoulos, M. Leeuwenhoek, C. Koks and M. P. Allan, *Imaging doubled shot noise in a Josephson scanning tunneling microscope*, Phys. Rev. B **100**, 104506 (2019), doi:10.1103/PhysRevB.100.104506.
- [53] J.-F. Ge, K. M. Bastiaans, D. Chatzopoulos, D. Cho, W. O. Tromp, T. Benschop, J. Niu, G. Gu and M. P. Allan, Single-electron charge transfer into putative Majorana and trivial modes in individual vortices, Nat. Commun. 14, 3341 (2023), doi:10.1038/s41467-023-39109-w.
- [54] J.-F. Ge, K. M. Bastiaans, J. Niu, T. Benschop, M. O. Larrazabal and M. P. Allan, *Direct visualization of quasiparticle concentration around superconducting vortices*, Appl. Phys. Lett. **125**, 252601 (2024), doi:10.1063/5.0240672.
- [55] M. Ruby, F. Pientka, Y. Peng, F. von Oppen, B. W. Heinrich and K. J. Franke, *Tunneling processes into localized subgap states in superconductors*, Phys. Rev. Lett. **115**, 087001 (2015), doi:10.1103/PhysRevLett.115.087001.
- [56] U. Thupakula, V. Perrin, A. Palacio-Morales, L. Cario, M. Aprili, P. Simon and F. Massee, *Coherent and incoherent tunneling into Yu-Shiba-Rusinov states revealed by atomic scale shot-noise spectroscopy*, Phys. Rev. Lett. **128**, 247001 (2022), doi:10.1103/PhysRevLett.128.247001.
- [57] J. P. Cuperus, D. Vanmaekelbergh and I. Swart, *Data package from article 'Non-topological edge-localized Yu-Shiba-Rusinov states in CrBr*₃/*NbSe*₂ *heterostructures*', Data publication platform of Utrecht University (2025), doi:10.24416/UU01-LB70QM.